A FULLY AUTOMATED DERIVATION OF STATE-BASED EIGENTRIPHONES FOR TRIPHONE MODELING WITH NO TIED STATES USING REGULARIZATION

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ABSTRACT

Recently we proposed an alternative method called eigentriphone to solve the data insufficiency problem in triphone acoustic modeling without the need of state tying. The idea is to treat the acoustic modeling problem of infrequent triphones (“poor triphones”) as an adaptation problem from the more frequent triphones (“rich triphones”): firstly, an eigenbasis is developed over the rich triphones that have sufficient training data and the eigenvectors are called eigentriphones; then the poor triphones are adapted in a fashion similar to eigenvoice adaptation. Since, in general, no states are tied in our method, all triphones (states) are distinct so that they can be more discriminative than tied-state triphones.

In our previous work, the number of eigentriphones was determined in advance with a set of development data. In this paper, we investigate simply using all of them with the help of regularization to naturally penalize the less important ones. In addition, the model-based eigenbasis is replaced by three state-based eigenbases. Experimental evaluation on the WSJ 5K task shows that triphone models trained using our new eigentriphone approach without state tying perform at least as well as the common tied-state triphone models.

Index Terms: Eigenvoice, adaptation, eigentriphone, regularization.

1. INTRODUCTION

In (context-dependent) triphone hidden Markov modeling (HMM), parameter sharing is generally applied to ensure that there are sufficient training data for the robust estimation of the shared parameters. In particular, state tying using a phonetic tree [2] is a commonplace, and good recognition performance is always reported. Nevertheless, one plausible problem with state tying is that the tied-state triphones may become less discriminative because a state of one triphone may be identical to a state of another triphone, causing confusion between the two triphones during recognition.

Recently, Chang and Glass proposed a back-off discriminative acoustic modeling method based on broad phonetic classes [3]. In their work, the acoustic score of a triphone is computed from an interpolation between the native triphone model that is based on single-phone contexts and triphone models that are based on broad-phonetic-context classes. Although it can guarantee that every triphone has a distinct acoustic score, acoustic-phonetic knowledge is required to derive the broad phonetic classes. How to get the “optimal” (if there is one) broad phonetic classes for any modeling units (triphonics, syllables, etc.) requires further investigation.

Last year, we proposed an alternative approach to context-dependent acoustic modeling called eigentriphone [5]: an eigenbasis is computed from the frequent triphones of each base phone, and acoustic modeling of infrequent triphones is treated as an adaptation problem using the established eigenbases. Our method is similar to [3] in that, since states are generally not tied in our eigentriphone method, all triphones in our method are distinct from each other. On the other hand, our method has the advantage that no phonetic knowledge is required, and the whole method is data-driven and can be fully automated from the derivation of the eigenbases to the determination of the number of eigentriphones and the parameter estimation of the final triphone models.

Our method is motivated by the eigenvoice adaptation method [4]. Our eigentriphones are analogous to the eigenvoices in the eigenvoice adaptation method, but whereas there is only one eigenbasis in eigenvoice adaptation, we have 39 eigenbases — one eigentriphone basis for each of the 39 base phones. Furthermore, the selected number of eigentriphones represents the dimension of the eigentriphone-space, which can be determined using a set of development data. In our previous work [5], all triphones of the same base phone i use the same number of eigentriphones $K_i$ (though the value of $K_i$ varies with different base phones) for computational simplicity. Presumably, the value of $K_i$ should vary with different triphones of the same base phone depending on their amount of training samples. In this paper, we would like to avoid making a hard decision on the number of eigentriphones. Instead, we investigate the use of regularization to make a soft decision on the number of eigentriphones; the regularization term will naturally penalize the less important eigentriphones. In addition, besides other minor changes, the previous model-based eigentriphones are replaced by state-based eigentriphones since parameter sharing at the state level is usually more effective than parameter sharing at the model level [2].

This paper is organized as follows. In Section 2, we will first review our original model-based eigentriphone acoustic modeling approach, and then describe how the procedure is modified using regularization so that it is now fully automated. That is followed by experimental evaluation in Section 3 and conclusions in Section 4.

2. STATE-BASED EIGENTRIPHONES

We will first review the derivation procedure of model-based eigentriphones, and then describe the proposed improvements.

2.1. Derivation of Model-based Eigentriphones

Fig. 1 shows an overview of the model-based eigentriphone approach that we previously proposed in [5] for the estimation of the infrequent or “poor” triphones. The derivation procedure of eigentriphones is similar to that of eigenvoices in the eigenvoice adaptation method [4] except that (a) speaker-dependent models in eigenvoice
are replaced by triphone models, and (b) whereas eigenvoice adaptation creates only one single set of eigenvoices for any speakers, a set of eigentriphones is created for each base phone (or monophone). Thus, since there are 39 base phones in our systems, 39 sets of eigentriphones are derived.

The following procedure is repeated for each base phone $i$ using its triphones that appear in the training corpus.

**STEP 1:** Monophone hidden Markov model (HMM) of base phone $i$ is first estimated from the training data. Each monophone is a 3-state strictly left-to-right HMM, and each state is represented by an $M$-component Gaussian mixture model (GMM).

**STEP 2:** The monophone HMM of base phone $i$ is then cloned to initialize all its triphones. *No state tying is performed for the triphones.*

**STEP 3:** Categorize each of the triphones $q$ of base phone $i$ into one of the following two (possibly overlapping) sets based on its training sample counts $n_{iq}$ and two thresholds $\theta^R_m$ and $\theta^P_m$:

- the rich triphone set $\Omega^R_i$ if $n_{iq} \geq \theta^R_m$;
- the poor triphone set $\Omega^P_i$ if $n_{iq} < \theta^P_m$.

**STEP 4:** Only Gaussian means of triphones in the rich set are re-estimated. Thus, all triphones of the same base phone will share the same set of Gaussian covariances, mixture weights, and transition probabilities which are copied from the base phone HMM.

**STEP 5:** For each rich triphone $r \in \Omega^R_i$, create a triphone supervector $v_{ir}$ by stacking all Gaussian mean vectors from its three states as below.

$$v_{ir} = \begin{bmatrix} \mu_{ir11} & \mu_{ir12} & \cdots & \mu_{ir131} \\ \mu_{ir21} & \mu_{ir22} & \cdots & \mu_{ir231} \\ \mu_{ir31} & \mu_{ir32} & \cdots & \mu_{ir331} \end{bmatrix}$$ (1)

where $\mu_{irm,j} = 1, 2, 3$, and $m = 1, 2, \ldots, M$ is the mean vector of the $m$th Gaussian component at the $j$th state of triphone $r$. Similarly, a monophone supervector $m_i$ is created from the monophone model of the base phone $i$.

**STEP 6:** Collect all rich triphone supervectors $v_{i1}, v_{i2}, \ldots, v_{i[K_i]}$ as well as the monophone supervector $m_i$ of base phone $i$ together, and derive an eigenbasis from their correlation matrix using principal component analysis (PCA).

**STEP 7:** Arrange the eigenvectors $\{e_{ik}, k = 1, 2, \ldots, [\Omega^R_i]\}$ in descending order of their eigenvalues $\lambda_k$, and select the top $K_i$ eigenvectors so that they cover $\phi_i$ of the total variations. These $K_i$ eigenvectors are called eigentriphones of phone $i$. In general, different base phones have a different number of eigentriphones.

**STEP 8:** Now the supervector $v_{ip}$ of any poor triphone $p \in \Omega^P_i$ is assumed to lie in the eigenbasis spanned by the $K_i$ eigentriphones. Thus, we have

$$v_{ip} = m_i + \sum_{k=1}^{K_i} w_{ipk} e_{ik}$$ (2)

where $w_{ip} = [w_{ip1}, w_{ip2}, \ldots, w_{ipK_i}]$ is the eigentriphone coefficients vector of triphone $p$ in the “triphone space” of base phone $i$. Notice that the monophone supervector $m_i$ is used instead of the mean of supervectors in Eqn. (2) so that the poor triphone model may fall back to the monophone HMM in the worst case.

**STEP 9:** Estimate the eigentriphone coefficient vector $w_{ip}$ of the poor triphone $p$ by maximizing the likelihood of its training data. Finally, the Gaussian mean of the mixture at the $j$th state of triphone $p$ can be obtained from $v_{ip}$ as

$$\mu_{ipjm} = m_{ijm} + \sum_{k=1}^{K_i} w_{ipk} e_{ikjm}.$$ (3)

### 2.2. Investigation Issue #1: Soft Decision on the Number of Eigentriphones using Regularization

In our previous paper [5], the number of eigentriphones $K_i$ is determined in advance using a separate development set. There are two drawbacks with the old scheme:

- In general, the value of $K_i$ should also depend on the amount of available training data of each poor triphone $p$ of base phone $i$. For triphones with more training data, a larger $K_i$ will give them a better model.
- It is not clear how to set the threshold $\phi_i$, which determines the value of $K_i$. In [5], it is determined empirically using development data and the procedure is time-consuming.

Here, we attempt to make a soft decision on the value of $K_i$ by using all eigentriphones with the help of regularization so that the less important eigentriphones are automatically de-emphasized. We define a new penalized log likelihood function $Q(w_{ip})$ for the estimation of eigentriphone coefficient vector $w_{ip}$ as follows:

$$Q(w_{ip}) = L(w_{ip}) - \beta R(w_{ip})$$ (4)

where $\beta$ controls the relative importance of the regularization term $R(\cdot)$ compared with the likelihood term $L(\cdot)$. The log likelihood of the training data is given by

$$L(w_{ip}) = \text{constant} - \sum_{j,m,t} \gamma_{ipjm}(t)(x_t - \mu_{ipjm}(w_{ip}))^T C^{-1}_{ipjm}(x_t - \mu_{ipjm}(w_{ip}))$$

where $C_{ipjm}$ and $\gamma_{ipjm}(t)$ are the covariance and occupation probability of the $m$th Gaussian at the $j$th state of poor triphone $p$ of base phone $i$ given observation $x_t$.

We investigate the following regularization term

$$R(w_{ip}) = \sum_{k=1}^{[\Omega^R_i]} \frac{w_{ipk}^2}{\lambda_k}$$ (5)

with the following considerations:
• The likelihood term should be more dominant when there are more training data. In particular, when a large amount of training data is available, the "adapted" triphone model should converge to its context-dependent estimate.
• Because of Eqn.(2), the adapted triphone model will converge to the monophone model for small amount of training data.
• Each eigentriphone coefficient, \( w_{ipk} \), is scaled by the inverse of its corresponding eigenvalue so that a less informative eigentriphone will have less influence on the adapted model.

Differentiating the optimization function \( Q(w_{ipk}) \) of Eqn.(4) w.r.t. each eigentriphone coefficient, and setting each derivative to zero, we have,

\[
\sum_{n=1}^{[\Omega_i^k]} A_{ipkn} w_{ipjm} + \beta w_{ipk} = B_{ipk} \quad \forall k = 1, 2, \ldots |\Omega_i^k| 
\]

where

\[
A_{ipkn} = \sum_{j,m} e_{ipkm} e_{ipjm} - \frac{1}{M} \sum_{t} \gamma_{ipjt}(t) \Omega_{ijm}(t) 
\]

\[
B_{ipk} = \sum_{j,m} e_{ipkm} e_{ipjm} - \frac{1}{M} \sum_{t} \gamma_{ipjt}(t)(x_t - m_{ipjm}) \Omega_{ijm}(t) 
\]

The eigentriphone coefficients may be easily found by solving the system of \( |\Omega_i^k| \) linear equations represented by Eqn.(6), and the Gaussian means of the new model may be computed using Eqn.(3). The training data may be re-aligned using the new model, obtaining a new set of occupation probabilities \( \gamma_{ipjt}(t) \) so that the eigentriphone coefficients may be re-estimated. The procedure is repeated until the coefficients converge.

### 2.3. Investigation Issue #2: State-based Eigentriphones

The eigentriphone adaptation framework described so far uses the whole triphone model to construct a supervector, and we will call the resulting eigenvectors as model-based eigentriphones. Actually the construction unit can be very flexible. In this paper, we would like to investigate the performance of state-based eigentriphones which are obtained by creating three separate eigenbases, one from each state. Compared with model-based eigentriphones, state-based eigentriphones have 3 times more eigenbases, but the dimension of each state-based eigentriphone is 1/3 of a model-based eigentriphone.

### 2.4. Other Improvements

Re-estimation thresholds \( \theta^p \), \( \theta^m \), and \( \theta^r \) are further defined to control the re-estimation of triphone covariances, mixture weights, and transition probabilities respectively based on its sample count. That is, the quantity will only be re-estimated if the sample count of the triphone exceeds the respective threshold, otherwise, its value is simply copied from its monophone model.

### Table 1. Information of various WSJ data sets.

<table>
<thead>
<tr>
<th>Data Set</th>
<th>#Speakers</th>
<th>#Utterances</th>
<th>Vocab Size</th>
<th>OOV</th>
</tr>
</thead>
<tbody>
<tr>
<td>SI284</td>
<td>283</td>
<td>37,413</td>
<td>13,646</td>
<td>—</td>
</tr>
<tr>
<td>si_dt05_odd</td>
<td>10</td>
<td>248</td>
<td>1.260</td>
<td>0</td>
</tr>
<tr>
<td>Nov’92</td>
<td>8</td>
<td>330</td>
<td>1.270</td>
<td>0</td>
</tr>
<tr>
<td>Nov’93</td>
<td>10</td>
<td>215</td>
<td>1.004</td>
<td>0.29%</td>
</tr>
</tbody>
</table>
Table 2. Recognition word accuracy (%) of various systems on the WSJ 5K task using bigram language model. (The figure with an * is statistically and significantly better than its baseline result.)

<table>
<thead>
<tr>
<th>System</th>
<th>Nov’92</th>
<th>Nov’93</th>
</tr>
</thead>
<tbody>
<tr>
<td>tied-state triphone system</td>
<td>94.36</td>
<td>91.40</td>
</tr>
<tr>
<td>Baseline2</td>
<td>93.98</td>
<td>91.79</td>
</tr>
<tr>
<td>no state tying; only Gaussian means of rich triphones are re-estimated</td>
<td>93.50</td>
<td>90.83</td>
</tr>
<tr>
<td>+ state-based eigentriphone “adaption” of means for poor triphones</td>
<td>93.78</td>
<td>91.37</td>
</tr>
<tr>
<td>+ re-estimation of Gaussian variances, mixture weights, and transition probabilities when the respective re-estimation thresholds are met</td>
<td>94.53</td>
<td>92.44*</td>
</tr>
<tr>
<td>Baseline3</td>
<td></td>
<td></td>
</tr>
<tr>
<td>tied-state triphone system</td>
<td>96.45</td>
<td>93.89</td>
</tr>
<tr>
<td>state-based eigentriphone system</td>
<td>96.41</td>
<td>94.47</td>
</tr>
<tr>
<td>model-based eigentriphone system</td>
<td>96.47</td>
<td>94.44</td>
</tr>
</tbody>
</table>

Table 3. Recognition word accuracy (%) of various systems on the WSJ 5K task using trigram language model.

<table>
<thead>
<tr>
<th>System</th>
<th>Nov’92</th>
<th>Nov’93</th>
</tr>
</thead>
<tbody>
<tr>
<td>tied-state triphone system</td>
<td>96.45</td>
<td>93.89</td>
</tr>
<tr>
<td>state-based eigentriphone system</td>
<td>96.41</td>
<td>94.47</td>
</tr>
<tr>
<td>model-based eigentriphone system</td>
<td>96.47</td>
<td>94.44</td>
</tr>
</tbody>
</table>

3.4. Results and Discussions

The recognition performance of the various systems using bigram and trigram language models are shown in Table 2 and Table 3 respectively. It is observed that:

- The proposed state-based eigentriphone adaptation approach for the estimation of Gaussian means of the poor triphones with subsequent re-estimation of their remaining HMM parameters is effective. Each step gives incremental improvement over the Baseline3 system.
- Triphones without state-tying but trained using our proposed state-based eigentriphone approach outperform tied-state triphones on the Nov’93 test set, and perform slightly worse on the Nov’92 test set. However, most of the differences in their recognition accuracies are not statistically significant.
- Table 3 also compares the performance of state-based and model-based eigentriphones; they performed equally well. Since model-based eigentriphones result in fewer weights, they are preferred over the state-based eigentriphones.

3.5. Effect of Regularization for the Soft Decision on the Number of Eigentriphones

The performance of the proposed regularization method that makes a soft decision on the number of eigentriphones is compared with that of using a hard decision so that a fixed percentage, \( \phi e \), of the total variations are covered. The comparison result on the Nov’93 test set is shown in Fig 2. It can be seen that when a fixed number of eigentriphones are to be used, the number should not be too large or too small: when it is too large, the triphones with small amount of training data cannot be robustly estimated; when it is too small, the triphones with large amount of training data will be under-trained. The proposed regularization term helps avoid making the hard deci-

4. CONCLUSIONS AND FUTURE WORK

We successfully avoid making a hard decision on the number of eigentriphones to use in the eigentriphone adaptation framework for distinctive acoustic modeling with no state-tying. This is achieved by adding an appropriate regularization term in the objective estimation function of the eigentriphone coefficients so that eigentriphones with smaller eigenvalues are de-emphasized. The resulting recognition systems perform at least as well as tied-state triphone systems. In the current work, only Gaussian means of the poor triphones were “adapted”. We would like to investigate the adaptation of other HMM parameters, such as Gaussian variance and mixture weights in the future. We will also look at discriminative training of triphones trained using eigentriphone method. This can be done at two levels: (a) discriminative eigentriphones may be derived using discriminative component analysis methods such as LDA; (b) discriminative training methods such as MCE or MMI training.

5. ACKNOWLEDGEMENTS

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6. REFERENCES